

# Modeling condensation in nonhydrostatic cloud-scale models

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**ENERGY**

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Grabowski, W. W., and D. Jarecka, 2015: Modeling condensation in shallow nonprecipitating convection. *J. Atmos. Sci.*, **72**, 4661-4679.

Grabowski W. W., and H. Morrison, 2016: Modeling condensation in deep convection. *J. Atmos. Sci.* (in review).

## BULK MODEL OF CONDENSATION:

$$\frac{D\theta}{Dt} = \frac{L_v\theta}{c_p T} C_d$$

$$\frac{Dq_v}{Dt} = -C_d$$

$$\frac{Dq_c}{Dt} = C_d$$

$\theta$  - potential temperature

$q_v$  - *water vapor* mixing ratio

$q_c$  - *cloud water* mixing ratio

$L_v$  - latent heat of condensation/evaporation

$C_d$  - condensation rate

Note:  $\theta/T$  function of pressure only ( $\approx \theta_e/T_e$ , i.e., environmental hydrostatic pressure)

$C_d$  is defined such that cloud is always at saturation:

$$q_c = 0 \quad \text{if} \quad q_v < q_{vs}$$

$$q_c > 0 \quad \text{only if} \quad q_v = q_{vs}$$

where  $q_{vs}(p, T) = 0.622 \frac{e_s(T)}{p - e_s(T)}$  is the water vapor mixing ratio at saturation

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*Simple and easy: just 3 variables,*

*straightforward numerics*

*(e.g., no limit on time step...)*

$\theta$  - potential temperature

$q_v$  - water vapor mixing ratio

$q_c$  - cloud water mixing ratio

$L_v$  - latent heat of condensation/evaporation

$C_d$  - condensation mass

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## COMPREHENSIVE MODEL OF CONDENSATION:

$$\frac{D\theta}{Dt} = \frac{L_v\theta}{c_p T} C_d$$

$$\frac{Dq_v}{Dt} = -C_d$$

$$\frac{Dq_c}{Dt} = C_d$$

$$C_d \sim N \frac{dm}{dt}$$

$N$  - droplet concentration,  $\frac{dm}{dt}$  - droplet mass growth rate

$$\frac{dr}{dt} = A \frac{S}{r}, \quad A = A(p, T), \quad S - \text{supersaturation}$$

$$S = \frac{q_v}{q_{vs}} - 1$$

$$C_d \sim N r S$$

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**DOUBLE-MOMENT SCHEME:**

$$\frac{D\theta}{Dt} = \frac{L_v\theta}{c_p T} C_d$$

$$\frac{Dq_v}{Dt} = -C_d$$

$$\frac{Dq_c}{Dt} = C_d$$

$$\frac{DN_c}{Dt} = S_{act}$$

4 variables...

**BIN SCHEME:**

$$\frac{D\theta}{Dt} = \frac{L_v\theta}{c_p T} \sum_{i=1}^N C_d^{(i)}$$

$$\frac{Dq_v}{Dt} = - \sum_{i=1}^N C_d^{(i)}$$

$$\frac{Dq_c^{(i)}}{Dt} = C_d^{(i)} + S_{act}^{(i)}$$

$i = 1, N$  – number of bins

dozen(s) variables...

$$C_d \sim N r S$$

*More complicated:*

DOUBLE-MOMENT SCHEME:

BIN SCHEME:

- *Prediction of  $S$  (cumbersome!)*
- *Bin; dozens of variables*
- *More involved time integration, often time sub-stepping wrt dynamics needed*

$$\frac{D\theta}{Dt} = \frac{L_v \theta}{c_p T} C_d$$

$$\frac{Dq_v}{Dt} = -C_d$$

$$\frac{Dq_c}{Dt} = C_d$$

$$\frac{DN_c}{Dt} = S_{act}$$

$$\frac{D\theta}{Dt} = \frac{L_v \theta}{c_p T} \sum_{i=1}^N C_d^{(i)}$$

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$$\frac{Dq_c^{(i)}}{Dt} = C_d^{(i)} + S_{act}^{(i)}$$

$i = 1, N$  – number of bins

4 variables...

dozen(s) variables...

All single-moment bulk microphysical schemes and most double-moment bulk schemes use bulk condensation...

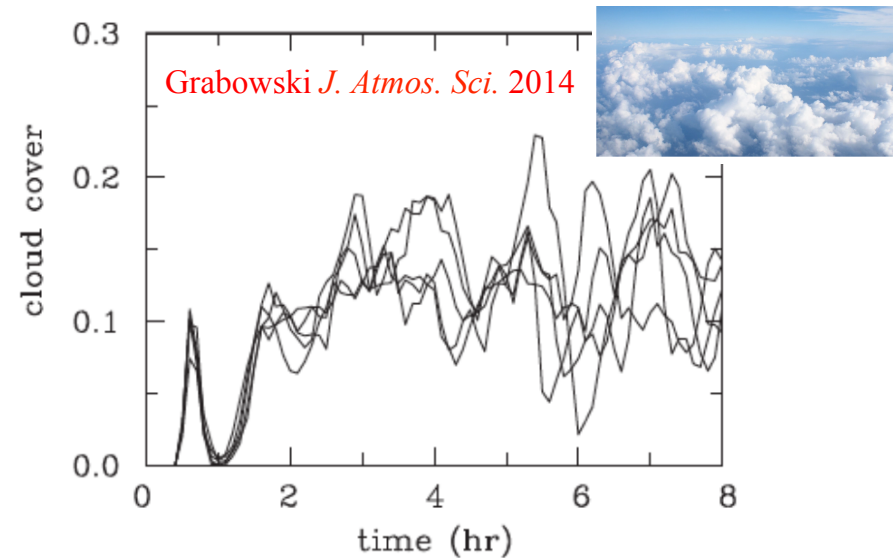


All single-moment bulk microphysical schemes and most double-moment bulk schemes use bulk condensation...

*Does it matter for the simulated cloud dynamics?*

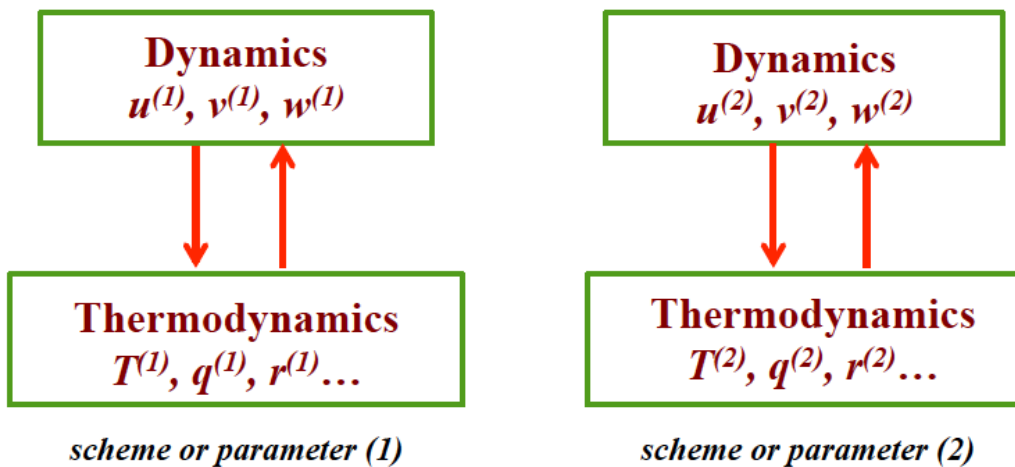
## Methodology:

Because of the nonlinear fluid dynamics, separating physical impacts from the effects of different flow realizations (“the butterfly effect”; Ed Lorenz) is nontrivial.



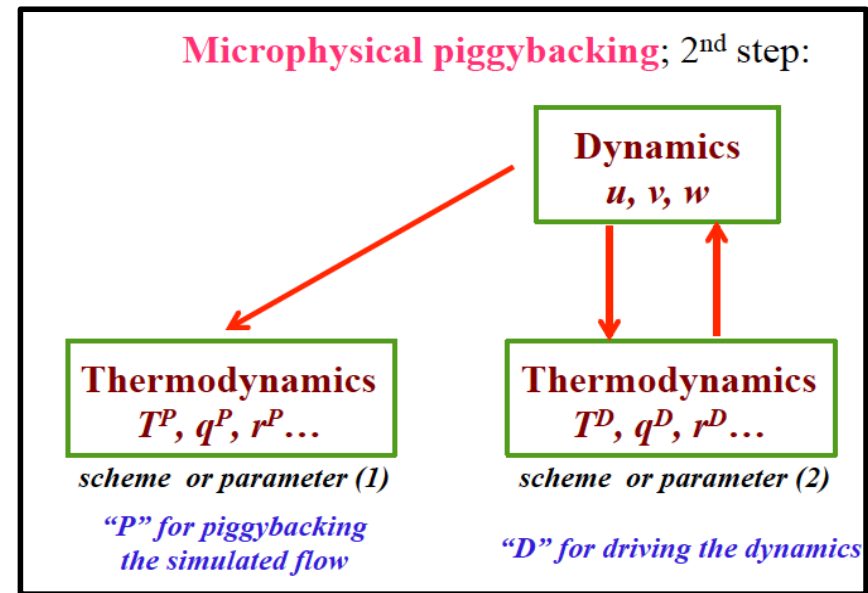
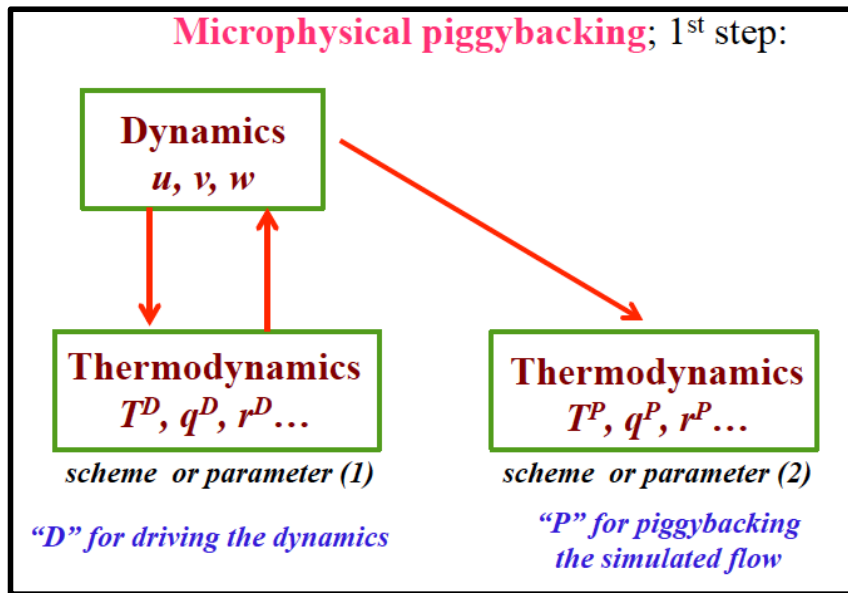
Evolution of cloud cover in 5 simulations of shallow cumulus cloud field. The only difference is in random small temperature and moisture perturbations at  $t=0$ .

**Traditional approach:** parallel simulations with different microphysical schemes or scheme parameters



The separation is traditionally done by performing parallel simulations where each simulation applies modified model physics.

# Novel modeling methodology: *the piggybacking*

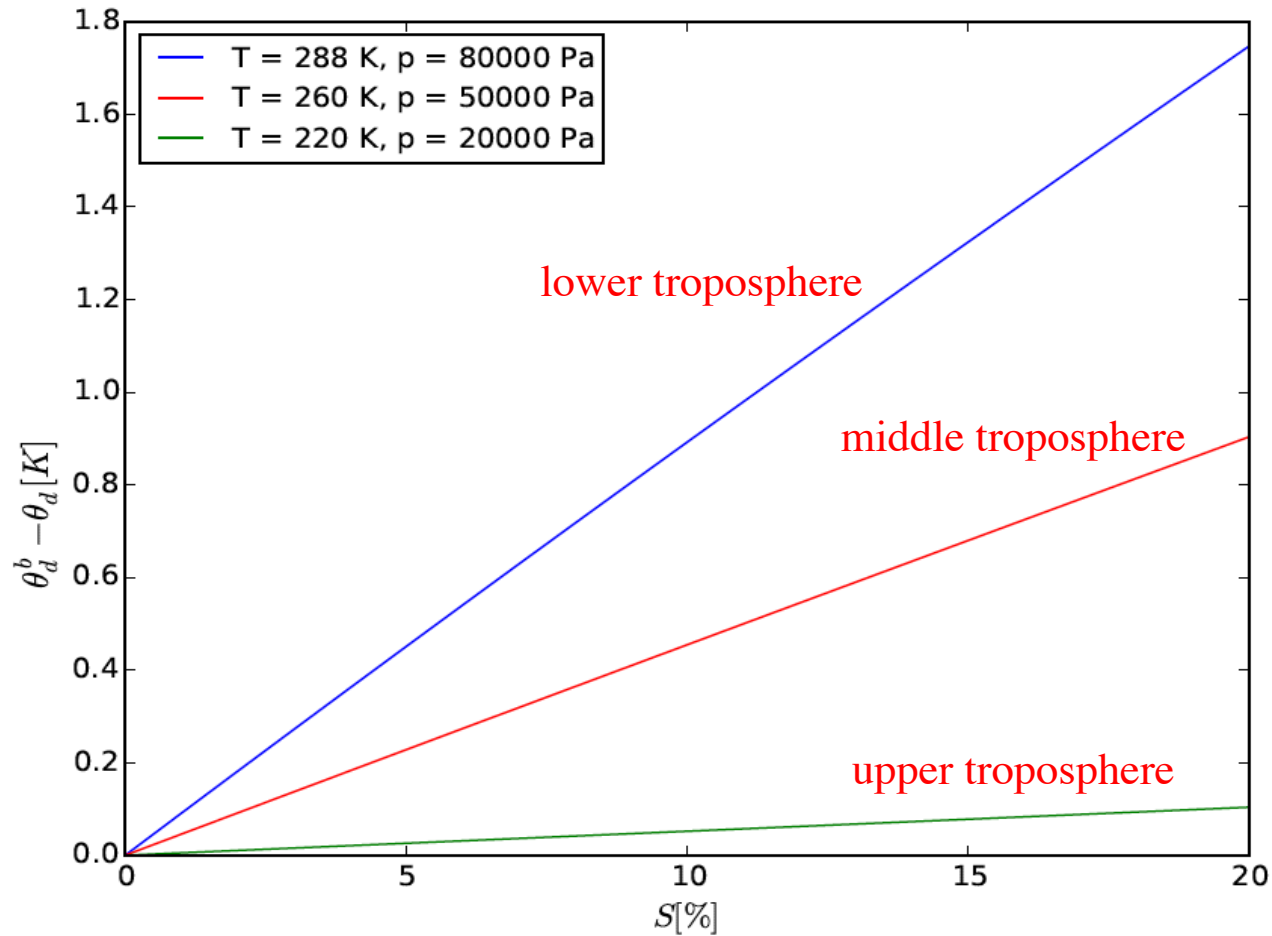


- Grabowski, W. W., 2014: Extracting microphysical impacts in large-eddy simulations of shallow convection. *J. Atmos. Sci.* **71**, 4493-4499.
- Grabowski, W. W., 2015: Untangling microphysical impacts on deep convection applying a novel modeling methodology. *J. Atmos. Sci.*, **72**, 2446-2464.
- Grabowski, W. W., and D. Jarecka, 2015: Modeling condensation in shallow nonprecipitating convection. *J. Atmos. Sci.*, **72**, 4661-4679.
- Grabowski, W. W., and H. Morrison, 2016: Untangling microphysical impacts on deep convection applying a novel modeling methodology. Part II: Double-moment microphysics. *J. Atmos. Sci.*, **73**, 3749--3770.
- Grabowski W. W., and H. Morrison, 2016: Modeling condensation in deep convection. *J. Atmos. Sci.* (submitted).

Theoretical considerations:  
impact of a finite supersaturation on cloud buoyancy

Grabowski and Jarecka *JAS* 2015

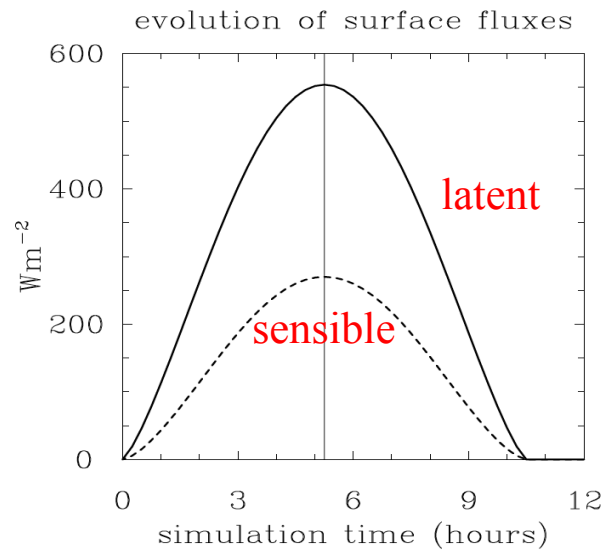
$$\theta_d^b \approx \theta_d + \Delta q \frac{L}{c_p} \left( \frac{p_o}{p} \right)^{R_d/c_p} (1 + \epsilon q_v - q_c)$$



Impact of finite supersaturations on cloud buoyancy in deep convection

## Daytime convective development over land: A model intercomparison based on LBA observations

By W. W. GRABOWSKI<sup>1\*</sup>, P. BECHTOLD<sup>2</sup>, A. CHENG<sup>3</sup>, R. FORBES<sup>4</sup>, C. HALLIWELL<sup>4</sup>,  
M. KHAIROUTDINOV<sup>5</sup>, S. LANG<sup>6</sup>, T. NASUNO<sup>7</sup>, J. PETCH<sup>8</sup>, W.-K. TAO<sup>6</sup>, R. WONG<sup>8</sup>,  
X. WU<sup>9</sup> and K.-M. XU<sup>3</sup>



Cloud-resolving simulations of LBA shallow to deep convection transition applying piggybacking methodology:

- 50 x 50 x 24 km<sup>3</sup> domain;
- 400 m horizontal gridlength;
- stretched grid in the vertical: 81 levels, ~50 m near the surface, ~300 m in the middle troposphere, ~600 m near the upper boundary;
- 4 s time step;
- run for 12 hrs, 3D fields saved every 6 min, time-averaged surface rain saved every 3 min.

Simulations with **double-moment bulk microphysics** of Morrison and Grabowski (*JAS* 2007, 2008a,b):

SPRE: predicting supersaturation  
SADJ: applying saturation adjustment

Vertical-velocity-based CCN activation parameterization  
(100, 200, 300, 400 cm<sup>-3</sup> droplet activated at 1, 5, 10 and 20 m s<sup>-1</sup>)

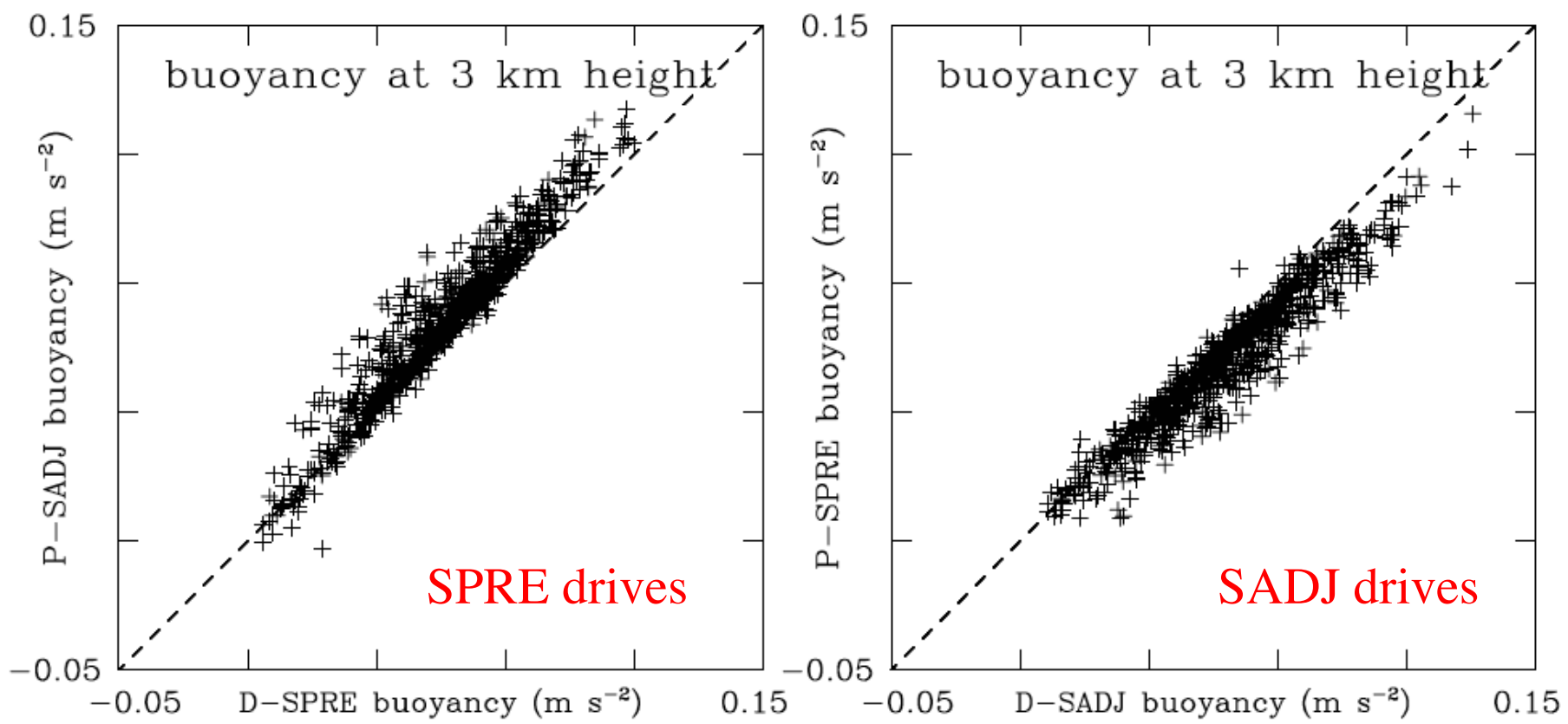
the same ice initiation in SPRE and SADJ

Piggybacking: D-SPRE/P-SADJ: SPRE drives, SADJ piggybacks  
D-SADJ/P-SPRE: SADJ drives, SPRE piggybacks

Five-member ensemble for each

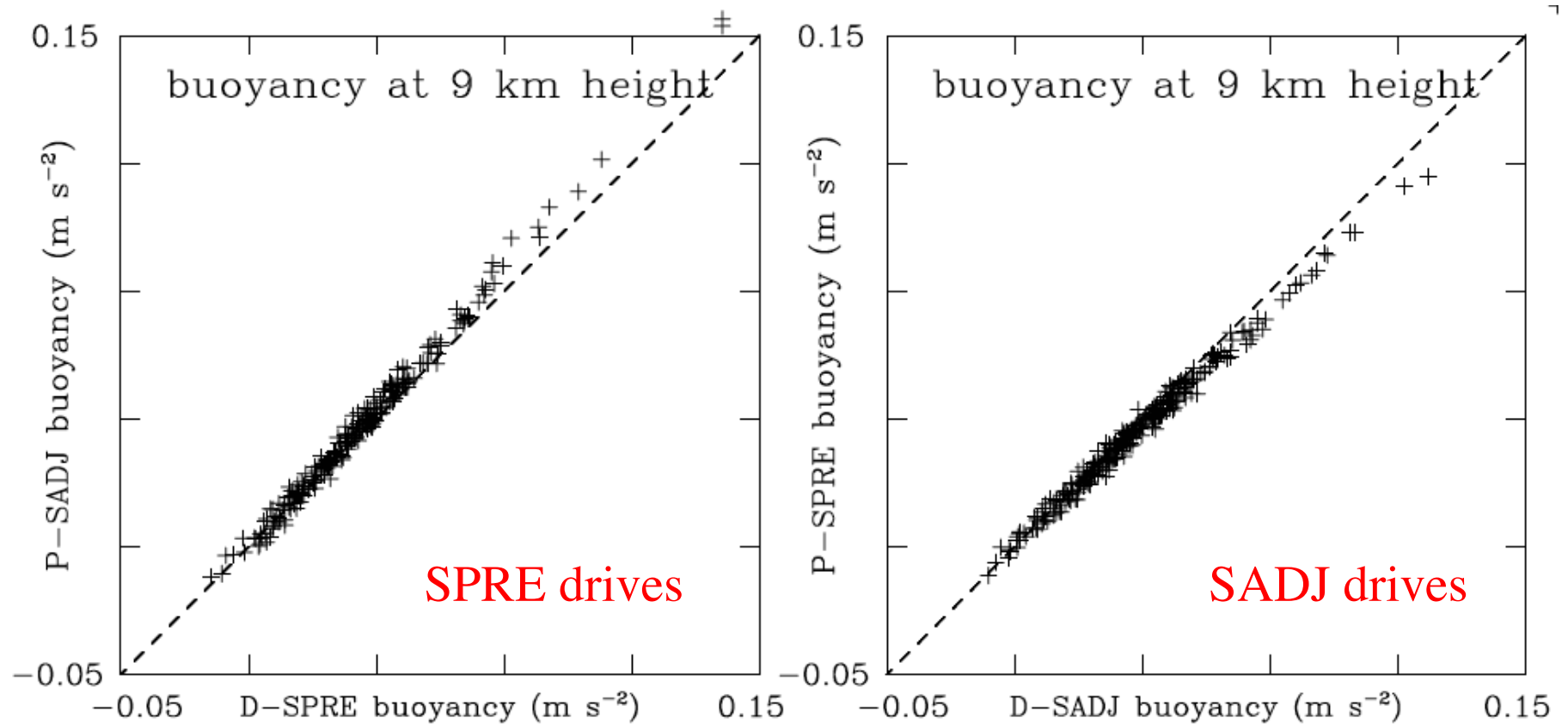


# Driver versus piggybacker buoyancy at 3 km (9°C)

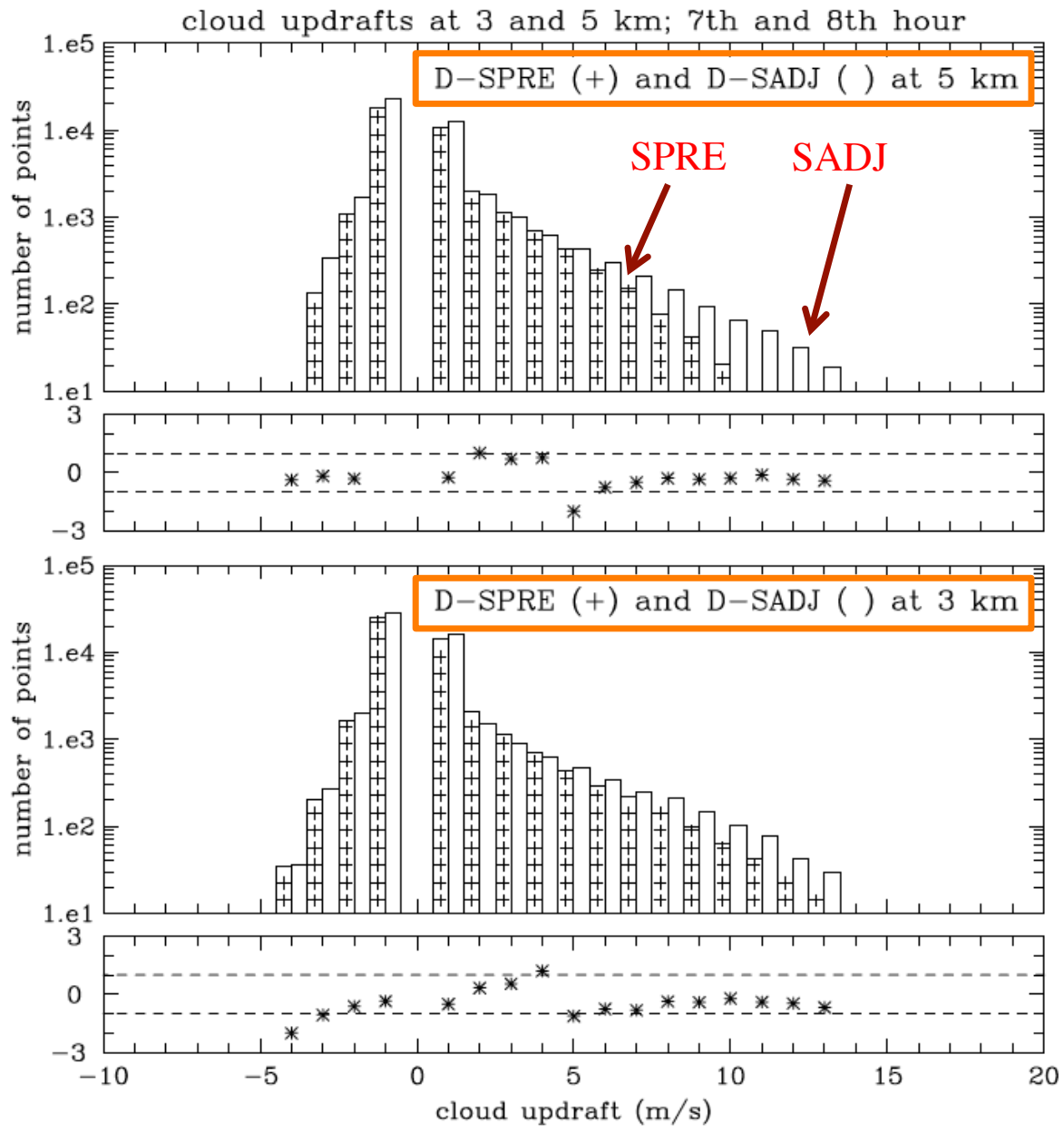


for gridpoints with  $w > 1$  m/s and  $q_c + q_r + q_{id} + q_{ir} > 0.1$  g/kg

# Driver versus piggybacker buoyancy at 9 km (-27°C)



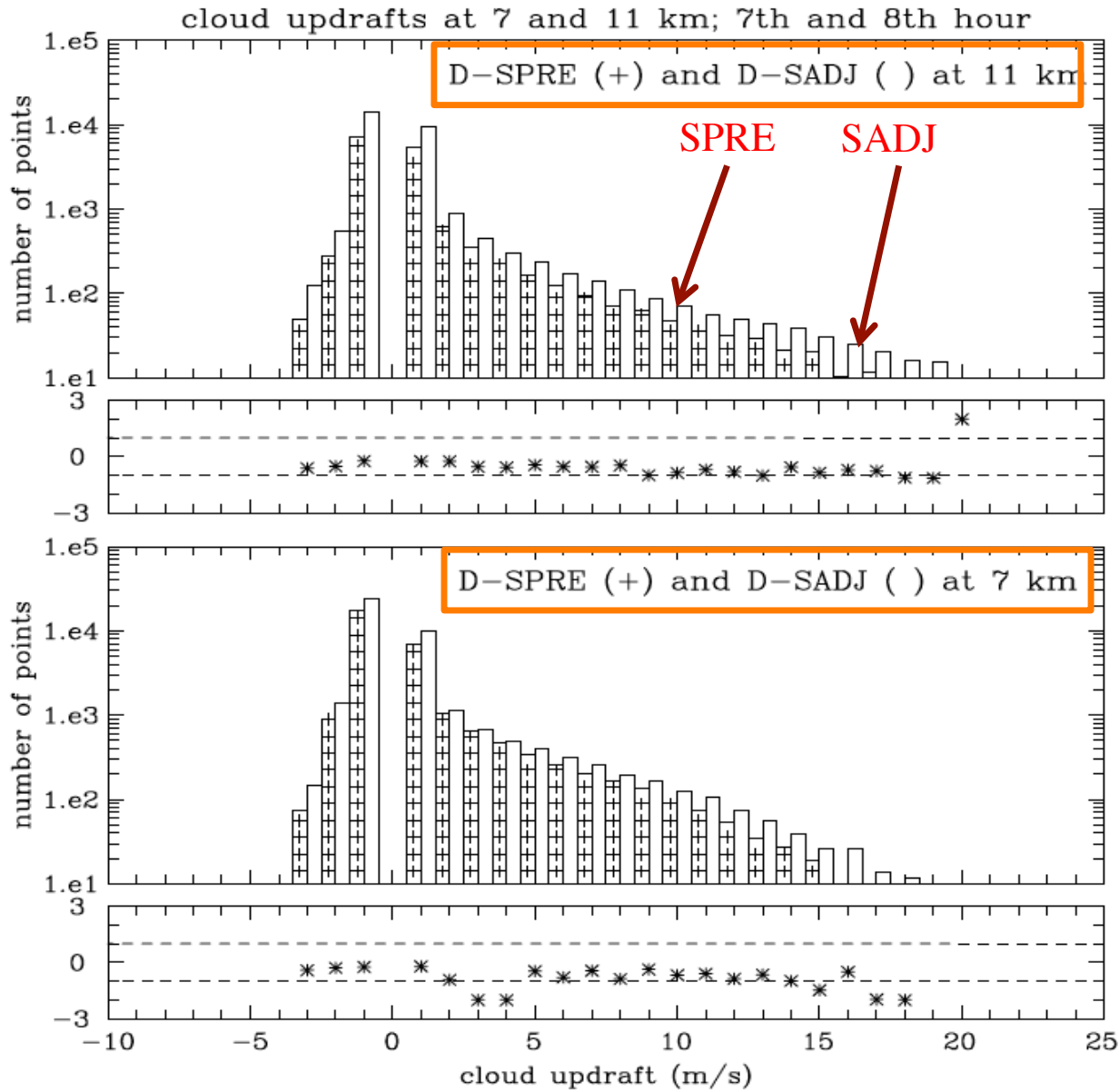
for gridpoints with  $w > 1$  m/s and  $q_c + q_r + q_{id} + q_{ir} > 0.1$  g/kg



5 km

3 km

Difference is statistically significant (at 95% confidence level) if the star is inside this range



11 km

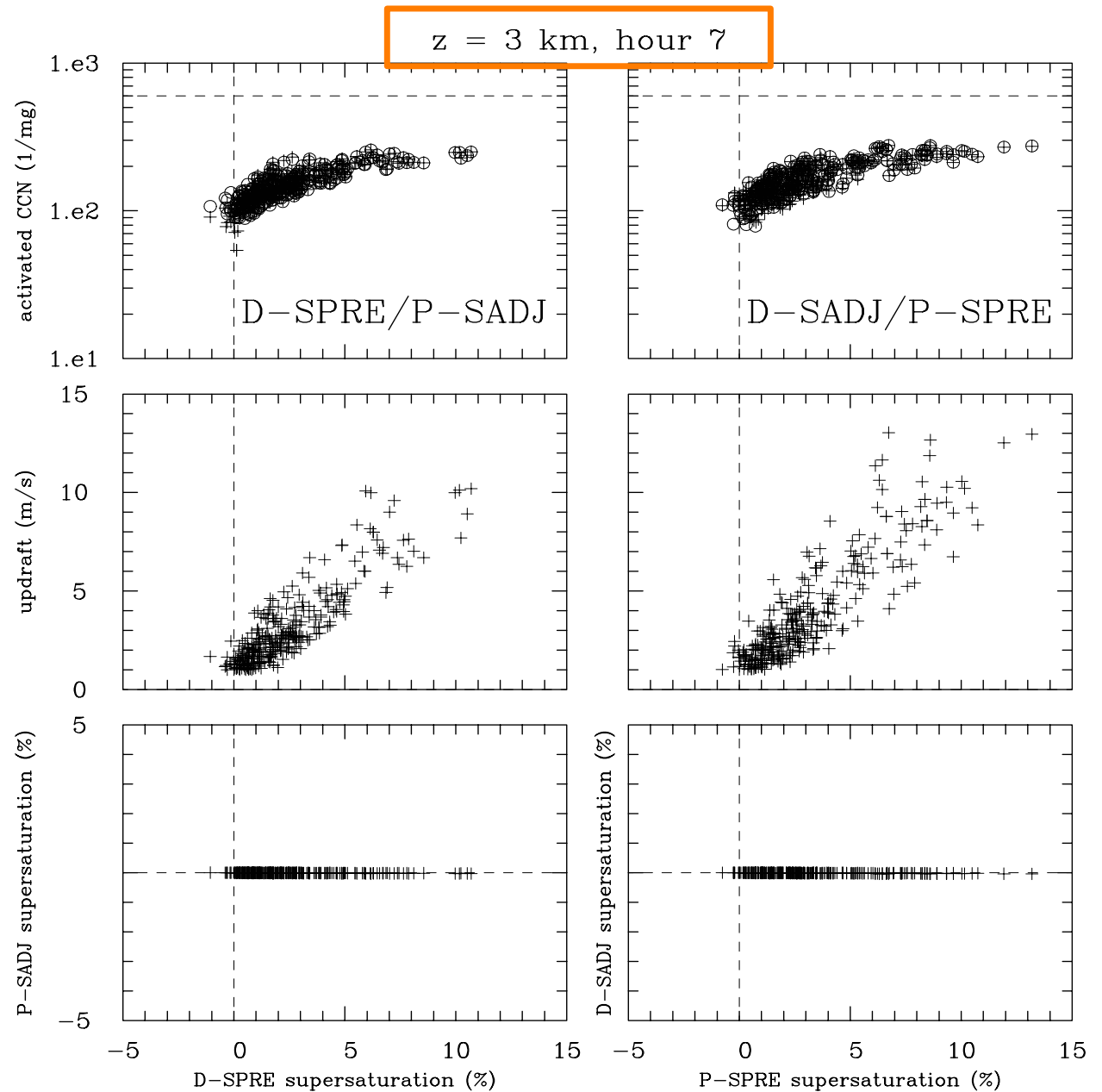
7 km

Difference is statistically significant (at 95% confidence level) if the star is inside this range

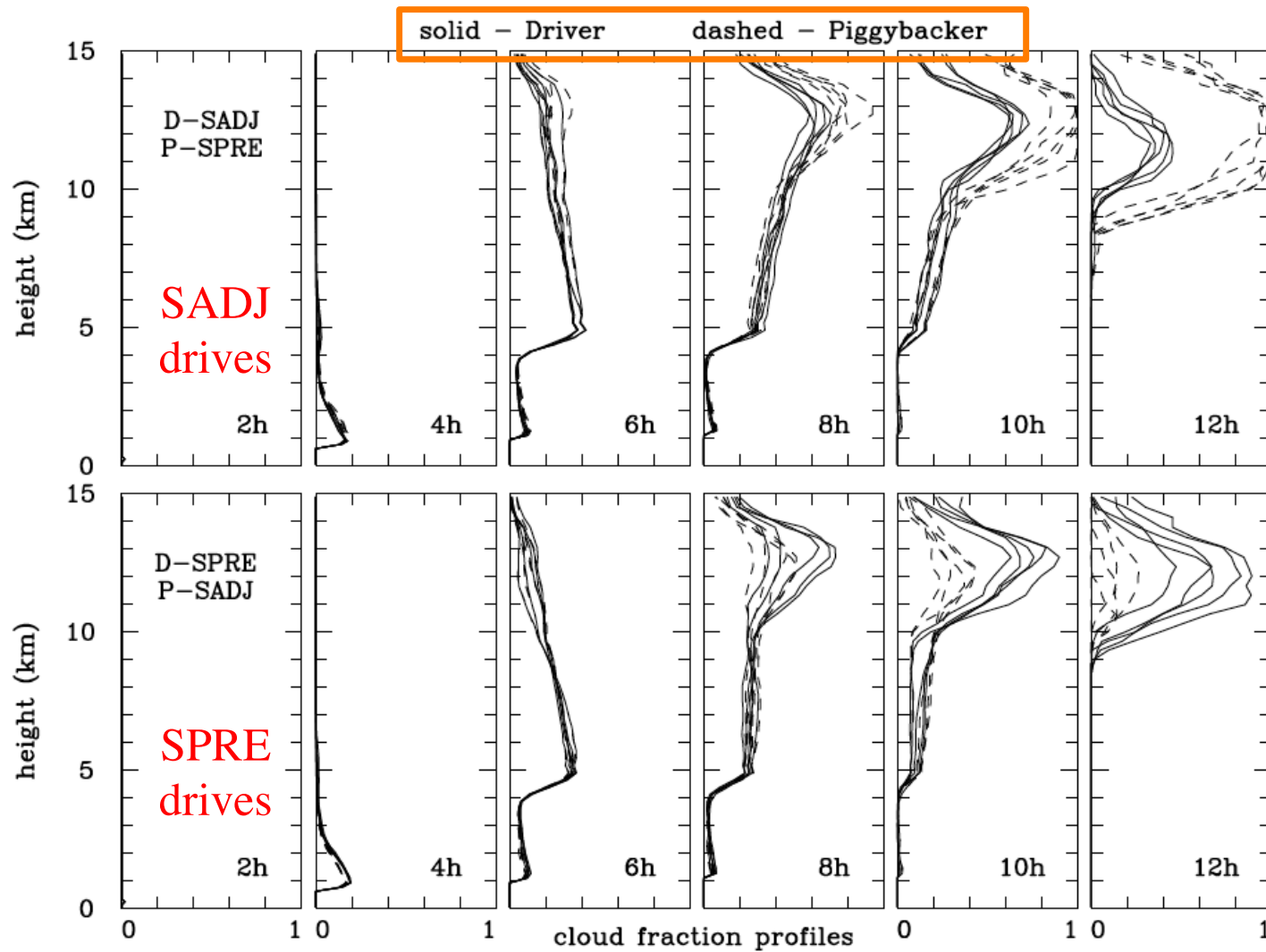
More CCN activated in stronger updrafts as expected...

Saturations increase with the updraft magnitude; stronger updrafts when SADJ drives...

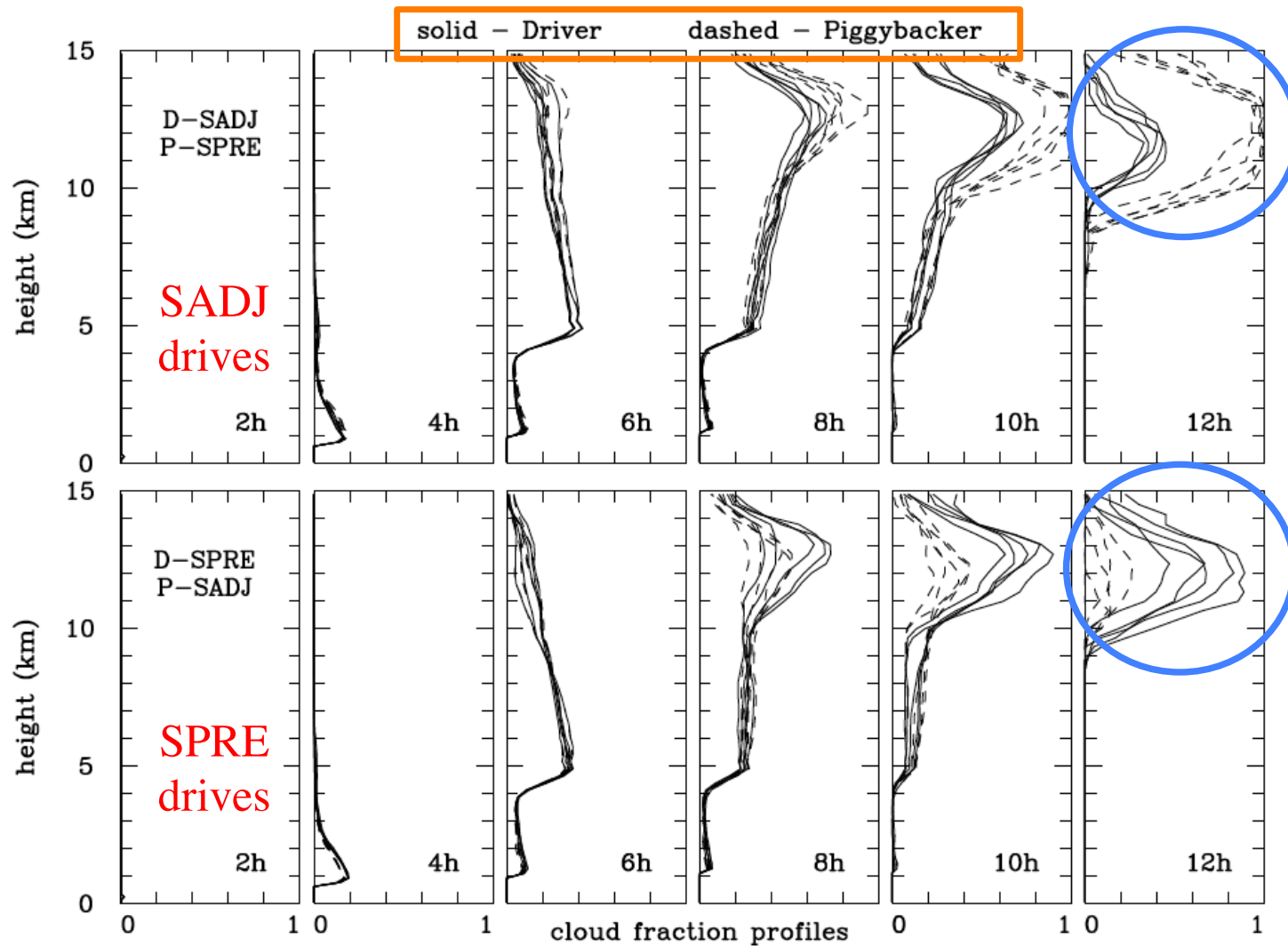
Saturation adjustment work correctly in SADJ; SPRE saturations are large...



evolution of cloud fraction profiles in 5-member ensembles  
D-SADJ/P-SPRE and D-SPRE/P-SADJ

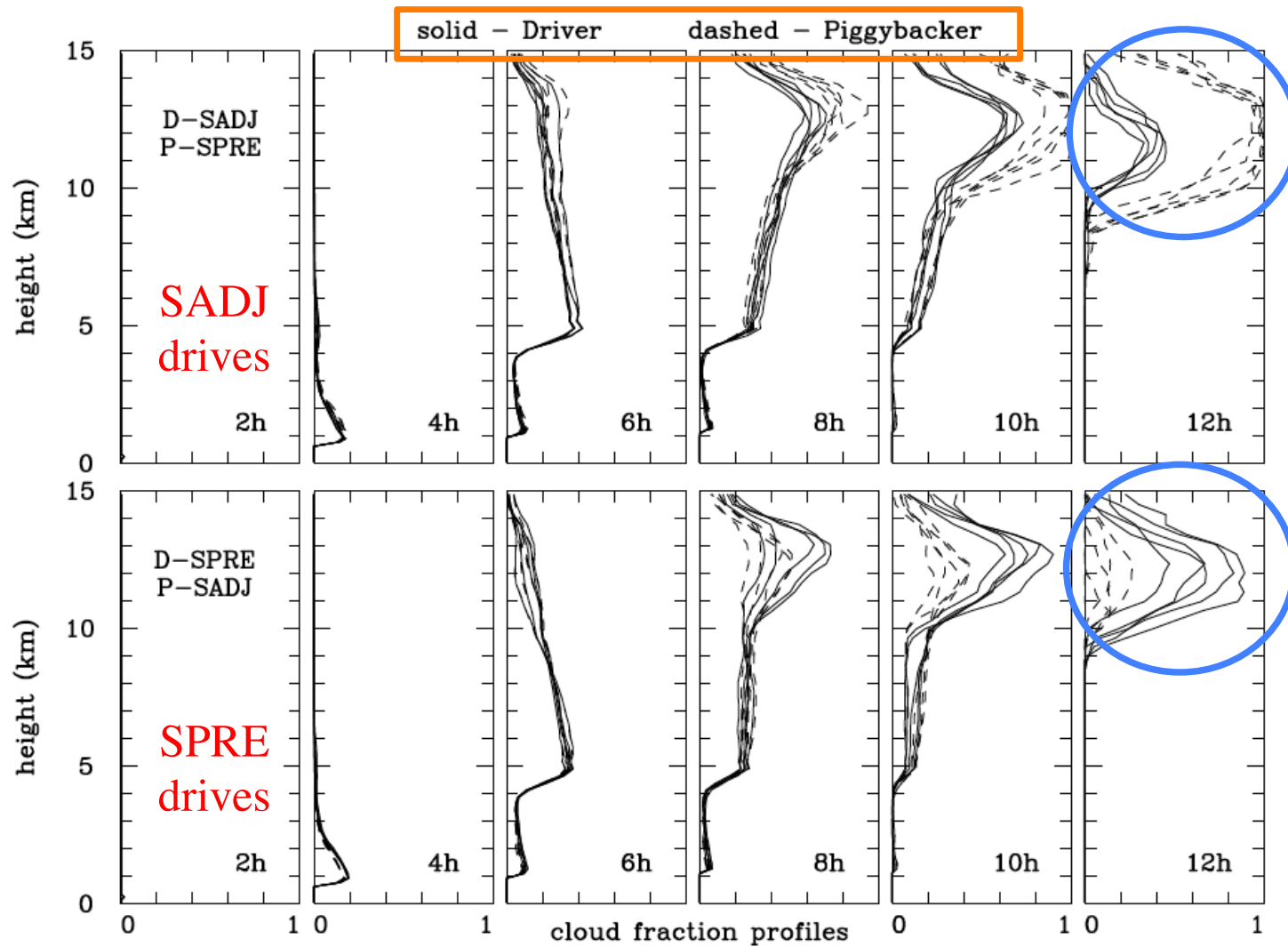


# evolution of cloud fraction profiles in 5-member ensembles D-SADJ/P-SPRE and D-SPRE/P-SADJ



SPRE has much larger fractions of anvil clouds after convection ceases regardless which drives...

evolution of cloud fraction profiles in 5-member ensembles  
D-SADJ/P-SPRE and D-SPRE/P-SADJ



larger fractions  
of anvil clouds  
are present when  
SADJ drives...



## **Conclusions:**

**Supersaturations in simulated deep convective updrafts are large, several percent. These are similar to pristine versus polluted CCN simulations in Grabowski and Morrison (*JAS* 2016).**

**These high supersaturations noticeably reduce cloud buoyancy and affect convective updraft statistics. Surface rainfall is about 3% larger when saturation adjustment is used.**

**There is a significant *microphysical* impact on convective anvils in the specific case considered and applying the specific supersaturation-dependent ice initiation scheme.**